

2nd Revised Edition

STATISTICS FOR MANAGERIAL DECISION MAKING



DR. S.K. KHANDELWAL

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Dr. S.K. KHANDELWAL

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▶ ABOUT THE BOOK

Statistics for Managerial Decision Making emphasizes the theory of statistics and applications of this theory for managerial decision making. The book is written in the most readable fashion to cater to the needs of such readers who do not have strong background of mathematics nor is it possible for them to acquire it now. The book reinforces the style where readers can independently understand the subject and solve practical problems. The reader friendly exposure of various topics will be of immense help to students to prepare for undergraduate and postgraduate examinations such as B.B.A., B.C.A., PGDBM, MBA, C.A., Company Secretary, I.C.W.A., M.Com., M.A.(Economics) and numerous post graduate programmes.

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- Problems cover all functions of management
- Very strong coverage of inferential statistics
- Includes latest techniques of Non-parametric tests
- Includes more than 1,500 problems

▶ ABOUT THE AUTHOR

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He has already authored a book titled "Business Statistics". In less than a year three reprints of the book show the popularity and acceptance of the book.



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