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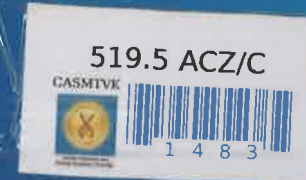
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Complete Business Statistics

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*To the memories of my father,
Captain E. L. Aczel, and my mother, Miriam Aczel*

Amir D. Aczel

To our families

Palanisamy Saravanan and Rohit Joshi

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